

Extracting decay rate ratios from photoluminescence quantum efficiency measurements in optoelectronic semiconductors

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Abstract

Recombination rates in optoelectronic semiconductors are typically recorded using time-intensive and expensive measurements. Here we present a method to extract decay rate ratios in a facile and rapid manner using only photoluminescence quantum efficiency measurements, which we demonstrate on halide perovskite thin film samples. We combine these ratios with time-resolved photoluminescence data to extract absolute recombination rates, with excellent agreement when our approach is benchmarked against the more time- and infrastructure-intensive technique of transient absorption spectroscopy. This approach also enables direct quantification of the ratio between total second order and radiative second order recombination rates. We demonstrate that radiative recombination is only a fraction of total second order recombination in the range of halide perovskite samples relevant for photovoltaics. We showcase the implications of rapid extraction of decay rates by extracting decay rate ratios on a microscale and by calculating the expected maximum efficiency of a solar cell fabricated from the measured perovskite films. We show that reducing first order losses will significantly improve solar cell efficiency for our samples until time-resolved photoluminescence lifetimes are longer than $\sim 1 \mu\text{s}$ (at low excitation pulse intensity), but at this point second order non-radiative recombination limits the efficiency of perovskite solar cells. This work represents a framework for rapidly screening optoelectronic semiconductors with techniques widely accessible to many research groups, identifies decay processes which would otherwise be missed, and directly relates the extracted values to predicted device performance metrics.

Introduction

Optoelectronic semiconductors, including halide perovskites, antimony selenide and bismuth-based materials, are being rapidly developed as the next generation of solar cells, light emitting diodes and X-ray scintillators [1–5]. For example, halide perovskite solar cell laboratory efficiencies now rival those of silicon [6]. In order to contextualize these improvements, identify remaining power loss pathways, and enable further advances, recombination mechanisms need to be fully quantified. Of particular importance is non-radiative recombination, which needs to be minimised in any developed device to maximize performance. Several methods have been used to understand excited charge carrier processes in films, including transient absorption spectroscopy (TAS), time-resolved photoluminescence (TRPL), terahertz spectroscopy, impedance spectroscopy and time-resolved voltage response [7–10]. Although powerful techniques, the majority are time-intensive, inaccessible to many academic and industry laboratories, and difficult to run successfully without specialised expertise, meaning recombination rates have only been fully quantified for a small subset of developing optoelectronic semiconductors, and material screening is not viable.

Here we introduce a method to rapidly quantify ratios between recombination rates in luminescent semiconductor thin film absorbers using just photoluminescence quantum efficiency (*PLQE*) measurements. By combining the *PLQE* measurements with complementary TRPL measurements – screenable techniques readily accessible to many laboratories – all recombination coefficients can be extracted. We demonstrate the technique on halide perovskite thin films and find excellent agreement when benchmarking our approach against TAS measurements. We use this technique to reveal that a non-radiative second-order recombination component is present, both in bulk and on the microscale, in the range of halide perovskite thin film compositions being utilised for solar cells, specifically in methylammonium lead iodide (MAPbI₃), mixed-cation mixed-halide formamidinium (FA)-containing mixtures (FA_{0.79}MA_{0.16}CS_{0.05})Pb(I_{0.83}I_{0.17})₃ and low bandgap FAPb_{0.5}Sn_{0.5}I₃ samples. We present evidence suggesting parasitic absorption and photon recycling alone cannot explain second order non-radiative recombination. We calculate the maximum efficiency of a solar cell fabricated from a measured MAPbI₃ film and demonstrate that second order non-radiative recombination will play an important role in device efficiency when time-resolved photoluminescence lifetimes (at low excitation fluence) are longer than 1 μs. Therefore second order non-radiative recombination is an important phenomenon to understand for ongoing device development. Our method will streamline materials screening

and optimisation for device performance using accessible techniques, and motivate further studies to explain unexpected recombination behaviour in semiconductors.

PLQE fitting model

Recombination rates of electrons and holes in optoelectronic semiconductors can be described by first, second and third order loss processes with respective rates a , b and c [8,11,12]. These rates are typically interpreted to be charge trapping (assuming most traps are rapidly filled [13]), second order processes (which typically describes radiative recombination of electrons and holes) and Auger recombination, respectively. An accessible technique to measure optoelectronic semiconductors, requiring only a laser, integrating sphere and detector, is the measurement of photoluminescence quantum efficiency – the ratio of emitted to absorbed photons [14]. Here we define an optoelectronic semiconductor to be one in which the number of excited electrons and holes (i.e. electrons and holes above background doping densities) are approximately equal, as generation rates produce excitation densities well in excess of trap densities. This corresponds to a semiconductor with a reasonably high (>0.1 %) external *PLQE*, as long as traps are not luminescent and thus do not contribute to this value. For example, trap densities are on the order of 10^{15} cm^{-3} in halide perovskites and 10^{13} cm^{-3} in copper indium gallium selenide thin films, so these assumptions are valid when excitation densities are larger than this, as in typical illumination conditions for solar cells and our measurements (see below) [15–17]. With these assumptions, when a region of the optoelectronic semiconductor is excited by a steady-state laser beam, the generation of charges is balanced by recombination. That is

$$G = an + bn^2 + cn^3. \quad (1)$$

Here G is the number of charges generated per unit time per unit volume in the film by an external laser beam and n is the number of excited charges per unit volume. For simplicity in the main text we present the case of a uniform excitation. However, in all modelling we use a (more physically realistic) model accounting for a Gaussian shaped beam. This Gaussian model is presented in the supplementary information and, without using this model, fitting errors of up to 30 % were found. We assume that charges are distributed uniformly from the front to the back of the thin film, as is the case in the halide perovskites probed here (where charges

redistribute from the front to the back of the film within a few ns following photoexcitation), [7,18,19]. This condition can be readily checked in other material families under analysis by testing whether TRPL measurements at different excitation fluences overlay when offset in time, following Richter et al. [8] If this does not hold diffusion lengths and/or surface recombination velocities should be included as an additional parameter, which is beyond the scope of this work, where the aim is to establish the validity of this approach (though we explore this further specifically for TRPL measurements below). We note that in all experiments carried out the incident laser beam was sufficiently large (>0.1 mm diameter) that lateral carrier diffusion effects can be ignored (as lateral diffusion lengths are on the order of $1 \mu\text{m}$ for halide perovskites studied here [18]).

The photon flux emitted to the surroundings (per unit area) is

$$D\eta_{esc}b_r(p_0n + n^2) \quad (2)$$

where D is the sample thickness, η_{esc} is the probability an emitted photon escapes the material, b_r the radiative recombination rate and p_0 a background electron or hole concentration which contributes to luminescence upon recombination with an excited charge. We note that $b = \eta_{esc}b_r + b_{nr}$, as has previously been discussed by others [20].

We can define the *PLQE* as the light emitted over the sample volume divided by the total (external) generation over the volume:

$$PLQE = \frac{D\eta_{esc}b_r(p_0n + n^2)}{D(an + bn^2 + cn^3)}. \quad (3)$$

We now consider what information can be extracted from *PLQE* measurements when varying the incident laser power. Importantly, ratios between recombination rates can be extracted from *PLQE* alone. We explain this by considering the substitution $n = \frac{\bar{n}}{\sqrt{\eta_{esc}b_r}}$ in equation 3, which reveals that there are four independent parameters in this equation (rather than the five seen above, which are inter-related). These parameters are

$$p_0\sqrt{\eta_{esc}b_r}; \frac{a}{\sqrt{\eta_{esc}b_r}}; \frac{b}{\eta_{esc}b_r}; \frac{c}{(\eta_{esc}b_r)^{\frac{3}{2}}}. \quad (4)$$

and equation 3 is converted to

$$PLQE = \frac{p_0\sqrt{\eta_{esc}b_r}\bar{n} + \bar{n}^2}{\frac{a}{\sqrt{\eta_{esc}b_r}}\bar{n} + \frac{b}{\eta_{esc}b_r}\bar{n}^2 + \frac{c}{(\eta_{esc}b_r)^{\frac{3}{2}}}\bar{n}^3}. \quad (5)$$

To fit equation 5, \bar{n} is calculated from the generation rate using equation 1, for some value of the free parameters shown in equation 4, and from this the $PLQE$ is calculated. The four free parameters are then varied until the modelled $PLQE$ optimally fits the experimental data. We developed a stochastic method to rapidly explore the parameter space and extract these ratios. Specifically, we randomised initial guesses of the parameters and ran the fitting algorithm many times. From this approach we obtain the parameters which give the best fit, and the spread of the parameters gives the error. Further details of the stochastic fitting approach used are described in Supplemental Material, Note 2 [21]. To avoid overfitting the data, we reduced the number of free parameters until we could fit the data with the data well with the fewest parameters (discussed further below). We emphasize that in addition to ratios between different order trapping rates, the ratio of total to radiative second order recombination, $\frac{b}{\eta_{esc}b_r}$ is extracted from $PLQE$ fitting alone, which we will explore further below. We note other standard spectroscopic analyses currently do not allow for the extraction of this parameter from a single measurement.

Fitting experimental $PLQE$ data

To test this fitting approach, and ascertain its reliability, we performed measurements on spin-coated passivated MAPbI₃ films of different thicknesses [22] (with samples increasing in thickness from sample 1 to sample 4, see methods). In the main text we present example data and fits, while all data and fits are presented in Figs. S16 –S22 and Supplemental Materials, Tables S3-5 [21]. Unless otherwise stated, samples were excited with 520 nm sources.

In Figure 1a we present the $PLQE$ of a MAPbI₃ film versus both incident laser intensity and excitation density n (as estimated from TAS and TRPL measurements, see Fig. S2 for details). As the laser intensity is increased the $PLQE$ rises from ~0.1 % to ~4 %. We fitted this $PLQE$ curve with several models based on equation 3, with different constraints on the parameters.

Specifically, we reduced the complexity of the fit until we were able to fit the data well with the fewest arbitrary constants (see Supplemental Material, Note 2 [21]). This allowed us to extract all ratios except $\frac{c}{(\eta_{esc} b r)^2}$ for all samples.

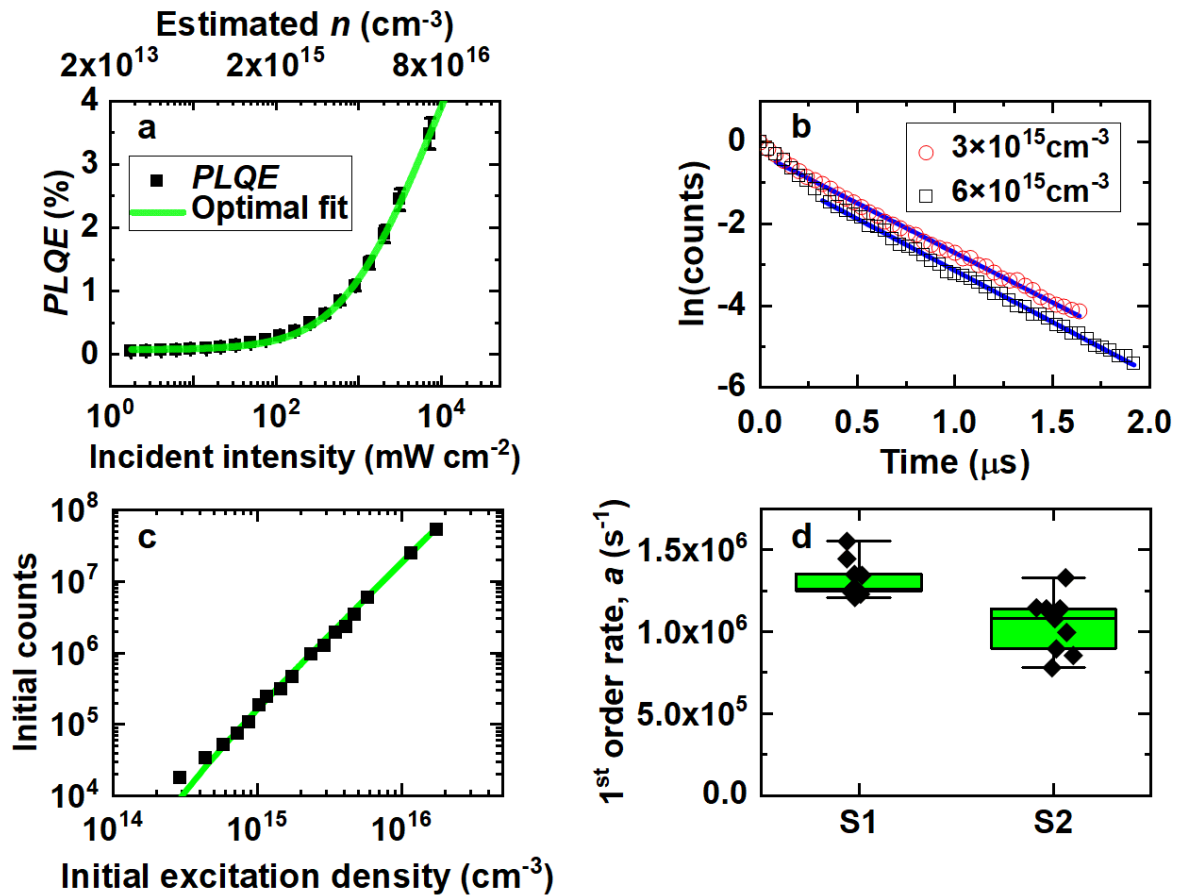


Fig. 1. a) Measured PLQE of a passivated MAPbI₃ film (sample 3) as a function of incident laser intensity, alongside the optimal fit to the data based on the model presented in equation 3. The excitation density, n , is estimated using values obtained from TAS and TRPL measurements (see Supplemental Material, Note 2 [21]). Error bars on PLQE data are calculated in accordance with the method outlined in Supplemental Material, Note 3 [21]. b) ln (TRPL counts) plotted as a function of time for two different initial excitation densities stated in the legend (for sample 1). Solid lines show fit to each data set. c) Scaling of initial time-resolved photoluminescence counts for sample 1 on a log scale, TRPL₀, for different excitation densities, used to estimate p_0 . d) First order decay rates extracted from fittings in b), for measurements at four different positions across the surface of sample 1 and 2.

To convert ratios extracted from PLQE into absolute decay rates, a second measurement is needed. Here we employ TRPL, an accessible technique in many research labs, where the

change in sample photoluminescence following photoexcitation is monitored, allowing values for p_0 and a to be obtained. During our proof of concept measurements we used a laser beam with a 1 kHz repetition rate, which is long enough for most charge traps to be depopulated in halide perovskites (on the order of 10-100 μs [23,24]). Our modelling can be readily extended to systems with faster repetition rates.

Extracting absolute decay rates

At low excitation densities, it can be approximated that $\frac{dn(x,y)}{dt} = -an(x,y)$, where t is time. As the photoluminescence is due to recombination of excited electrons and holes (i.e, $TRPL \propto n^2$), it can be shown that

$$\ln(TRPL(t)) = k - 2at \quad (6)$$

where k is an arbitrary constant. In Figure 1b we plot $\ln(TRPL(t))$ versus time to extract a . For all spots measured we carried out two measurements with different initial excitation densities (as marked on plot) to ensure that our values of a were robust. It can be seen in Fig. 1b that at higher excitation density there is a faster initial drop in the signal. We attribute the faster decay component at higher excitation density to the effects of second-order recombination, but restrict our fits (equation 6) to the portion of the data which is linear, as shown on the plot.

Accounting for spatial variation in the laser beam (Supplemental Material, Note 4 [21]) it can be shown that, immediately following excitation, the initial TRPL signal is given by

$$TRPL_0 \propto \eta_{esc} b_r \left(p_0 P_{pu} + \frac{AP_{pu}^2}{2\pi x_0 y_0 D E_{ph} f} \right). \quad (7)$$

Here P_{pu} is the measured laser power, A the fraction of incident laser light absorbed by the sample (which is measured through a typical $PLQE$ measurement [14]), x_0 and y_0 describe the spatial distribution of the incident laser beam (see Supplemental Material, Note 2 [21]), E_{ph} the energy of a photon at the excitation wavelength and f repetition rate of the incident laser beam. The second term gives the initial excitation density multiplied by P_{pu} . This equation

again assumes that charges are uniformly distributed from the front to the back of the film, even at early times. We note that this is approximately justified as charges diffuse relatively rapidly from the front to the back of the film (on the order of a few ns at most) [7]. However, for the model to be more generalizable, we explore the case where charges have not redistributed in Supplemental Material, Note 5 [21]. Measuring the scaling of $TRPL_0$ against P_{pu} allows for the absolute value of p_0 to be estimated (or if below instrument resolution, an upper bound). We demonstrate this fitting approach in Fig. 1c for a MAPbI₃ sample. In all our measurements we were only able to place an upper bound on p_0 of approximately 10^{14} cm⁻³ (see Supplemental Material, Note 5 for details [21]), which is a reasonable value as MAPbI₃ films are generally thought to have low doping levels [25]. We measured 4 spots on two different samples to quantify the variation in a , as presented in Fig. 1d. We find decay rates are relatively uniform across the sample surface ($\sim\pm 25\%$ at most), in spite of notable morphological, compositional and thickness variations reported within samples resulting from lab-based solution processing of perovskite thin films [26]. This justifies our approach in combining values extracted from TRPL with those from *PLQE* measurements, even though different regions on the sample surface are measured. We compare p_0 values obtained from our combined *PLQE*/TRPL approach with upper bounds from TRPL measurements alone and find values from the combined approach are convoluted with trap densities (see in Supplemental Material, Note 5 for details [21]).

Benchmarking the extracted rates

We now benchmark our *PLQE*/TRPL approach by comparing values of $\eta_{esc}b_r$ and b with those obtained from TAS. TAS is a pump-probe measurement that is more specialised than *PLQE* or TRPL and requires more experimental infrastructure [27]. Importantly, n is directly measured as a function of time [28]. In all TAS measurements we ensured the pump beam was large compared to the probe beam so that a region of uniform excitation density was measured (Supplemental Material, Note 6 [21]). Within this region we can neglect spatial variation in the pump and probe beams and any carrier diffusion effects and state

$$\frac{dn}{dt} = -an - bn^2 - cn^3. \quad (8)$$

We measured TAS signals at excitation powers where Auger recombination, which was not ascertained in *PLQE* measurements, could be neglected. In this case we can approximate $c \approx 0$, which gives the following solution to equation 8 (presented in a form primed for fitting data)

$$\frac{1}{n} = \left(\frac{b}{a} + \frac{1}{n_i} \right) e^{at} - \frac{b}{a} \quad (9)$$

where n_i is the excitation density when $t = 0$. Furthermore, if we only focus on the region where second order recombination dominates then

$$\frac{1}{n} = \frac{1}{n_i} + bt. \quad (10)$$

Therefore, to fit the TAS data, we plotted $\frac{1}{n}$ versus time and fit the data with both equation 9 and equation 10 to extract values of b (Supplemental Material, Table S4 [21]), depending in each case on whether a could be reasonably extracted from the data. An example of these fitting approaches is presented in Fig. 2a. Again, for two samples we measured b at three different positions across the sample surface. We found that there was more significant variation in b values ($\sim \pm 33\%$) than the variation in a from TRPL measurements (Fig. S23). We attribute this uncertainty to the additional measurements that are required to extract b from TAS, specifically sample thickness and beam size. Therefore, we find that combining *PLQE* measurements with TRPL data introduces less error than with TAS values, validating our approach.

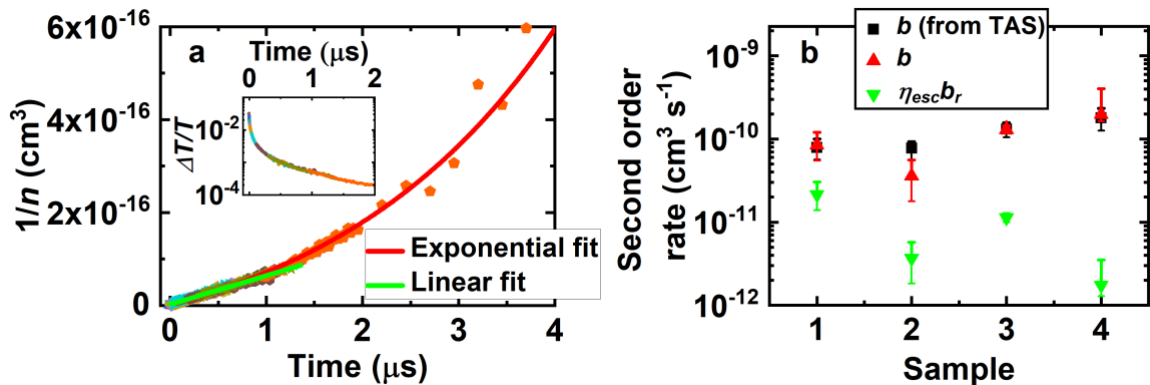


Fig. 2. a) $\frac{1}{n}$ versus time, as measured for sample 1 in TAS. Two fits to this data are shown – a linear fit to the high power data (equation 10), and an exponential fit (equation 9), to all the data. Inset shows recorded TAS signal with time (with each fluence offset in time to overlay the

decays). In both plots each colour represents a different incident fluence. b) All second order rates extracted from *PLQE/TRPL* and *TAS* measurements. For samples 1 and 2, *TAS* and *TRPL* error bars are obtained from the spread of data at different points on the surface, while for sample 3 and 4 20 % and 30 % error bars are assumed, based on quality of data taken.

To ascertain whether our *PLQE/TRPL* approach agrees with *TAS* measurements, we plot all second order rates ($\eta_{esc}b_r$ and b) in Fig. 2b. There is good agreement between values of b obtained from *PLQE/TRPL* and *TAS*, validating this analysis and fitting. Importantly, our *PLQE/TRPL* analysis also reveals that $\eta_{esc}b_r$ deviates from b values extracted in *TAS*, giving additional information and demonstrating a proportion of second order recombination is radiative. Notably, we were unable to fit *PLQE* data and obtain physically meaningful results with any model where $b = \eta_{esc}b_r$ (Supplemental Material, Note 2 [21]), confirming a real discrepancy between the radiative and total second-order recombination. Non-radiative second order recombination has previously been reported in halide perovskites using different techniques (see Richter et al. [8] and Staub et al. [29]) and thus we validate its presence here.

Extracting decay rate ratios on the microscale

We exemplify our framework can be extended to the microscale by local *PLQE* maps [30] at different (405 nm) laser excitation densities. This allows us to understand recombination occurring on the microscale using only a continuous wave laser (while a large spot size allows us to neglect diffusion effects). A local *PLQE* map of a passivated halide perovskite sample is presented in Fig. 3a and the spread of the extracted decay rates in Fig. 3b (we note these values cannot directly be compared with bulk measurements, see methods). Both first and second order decay ratios are relatively uniformly distributed about their central value (with upper and lower quartiles within $\sim 20\%$ of median value), meaning bulk results are representative of a large region of the sample and not due to a few abnormal regions. *PLQE* values are dominated by $\frac{a}{\sqrt{\eta_{esc}b_r}}$ (so are proportional to first order charge trapping), as is expected at the laser fluences used (see Fig. S29). We again find only a proportion of second order recombination is radiative. This approach opens up studies in which local recombination can be analysed using continuous wave microscopic setups.

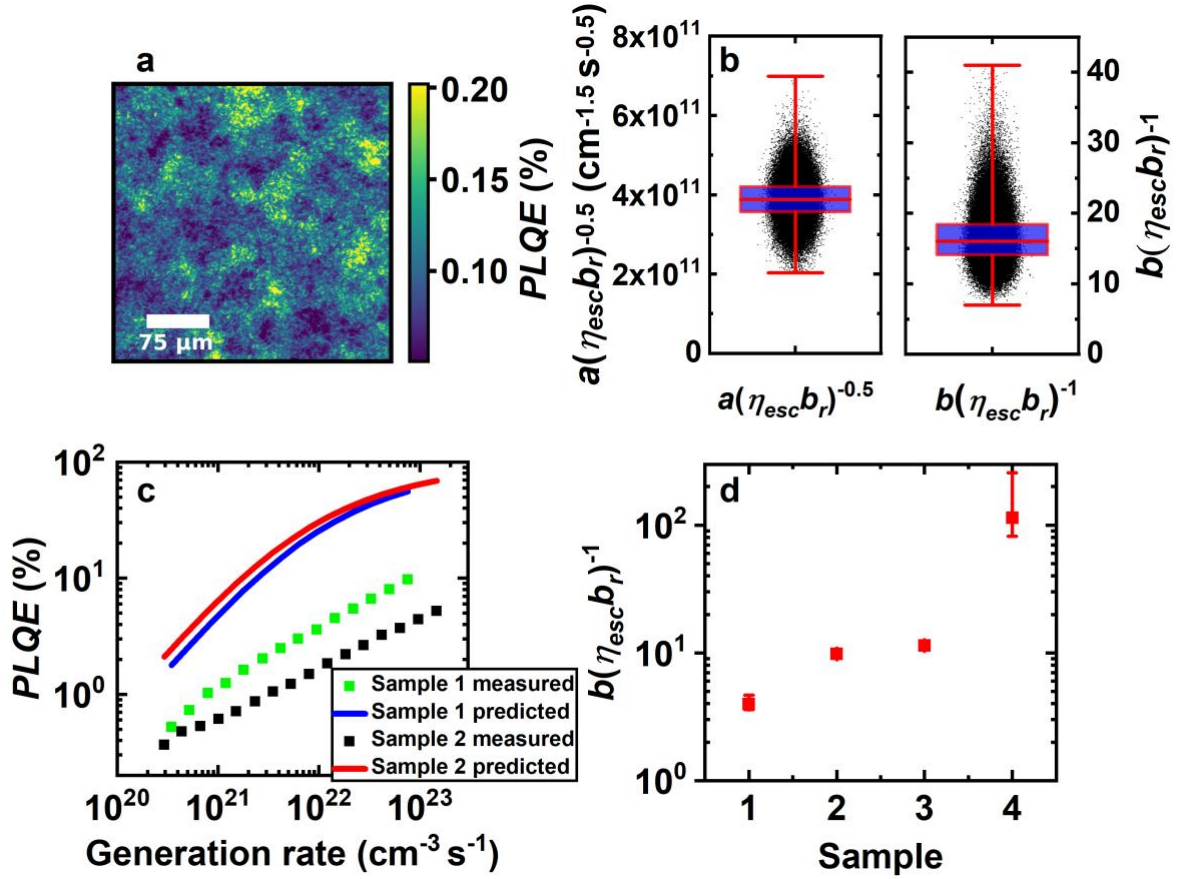


Fig. 3. a) Micro-PLQE map (for a 2 mWcm^{-2} excitation density) of a halide perovskite MAPbI_3 film (sample 3). The PLQEs with power were fitted for this map. Poor fits were removed from data (see Supplemental Material, Note 7 [21]), and results for $\frac{a}{\sqrt{\eta_{\text{esc}} b_r}}$ and $\frac{b}{\eta_{\text{esc}} b_r}$ are presented in b). Overlaid on these plots are the maximum, minimum, median, upper and lower quartiles as box and whisker plots. Samples were excited by a 405 nm beam. c) Measured PLQEs alongside those predicted from TAS and TRPL for samples 1 and 2. d) the ratio of $\frac{b}{\eta_{\text{esc}} b_r}$ from PLQE measurements for the four MAPbI_3 samples measured. We note that sample 4 was extremely thick ($>800 \text{ nm}$) and had low PLQE, so there is larger error in some values obtained. All PLQE error bars represent a 95 % confidence interval for fits (for samples 1 and 2, these are the maximum intervals obtained from any measurement on the sample surface, see Supplemental Material, Note 2 [21]).

Second order non-radiative recombination

To explore non-radiative second-order recombination further, we present in Figure 3c measured (macroscopic) PLQE for two samples, alongside predicted PLQEs from time-

resolved measurements (i.e. TRPL and TAS), using equation 3 and assuming only radiative second order recombination. There is a large discrepancy between measured and calculated values in this case. This discrepancy is more noticeable at higher generation rates, which have been explored less by others [16]. Furthermore, the variation in $\frac{b}{\eta_{esc}b_r}$ is significantly beyond what would be expected from outcoupling [31], as is shown by the ratio of $\frac{b}{\eta_{esc}b_r}$ in Figure 3d. To confirm observations of a fraction of the bimolecular component being non-radiative are not isolated to these passivated MAPbI₃ samples, we measured low-bandgap FAPb_{0.5}Sn_{0.5}I₃ and triple cation (FA_{0.79}MA_{0.16}CS_{0.05})Pb(I_{0.83}I_{0.17})₃ halide perovskites (where FA is formamidinium, see Figs. S24 and S25 for *PLQE* fits, and Supplemental Material, Table S4 for fit results [21]). We also found a discrepancy between b and $\eta_{esc}b_r$ on the same order of magnitude in these samples (see Supplemental Material, Table S3 for details [21]) suggesting the presence of non-radiative second order recombination is a general phenomenon in the range of halide perovskite sample compositions relevant for photovoltaic materials.

We consider (quantitatively) whether the non-radiative second order rate can be explained by experimental error or parasitic absorption processes in Supplemental Material, Note 7 [21]. Specifically, we consider (i) a systematic error in *PLQE* measurements, (ii) an error in thickness or power measurements, and (iii) parasitic absorption within the halide perovskite thin film. We demonstrate that none of these processes are able to fully explain non-radiative second order processes. We further explore non-radiative second order rates by noting that when samples 1 and 2 measured above were first fabricated the samples had relatively low *PLQEs* (< 1 %). However, after two months storage in a nitrogen flushed box, where some passivation occurs due to low levels of oxygen present [32], their *PLQEs* had risen significantly to those in Fig. S20. For sample 1, TAS measurements showed b changed from $(5.8 \pm 1.5) \times 10^{10} \text{ cm}^{-3}\text{s}^{-1}$ to $(8.5 \pm 2.0) \times 10^{11} \text{ cm}^{-3}\text{s}^{-1}$ over this time (Fig. S27). We were also able to measure $\frac{b}{\eta_{esc}b_r}$ reliably from *PLQE* before and after storage and obtained comparable values of $\eta_{esc}b_r$, of $(1.4 \pm 0.7) \times 10^{11} \text{ cm}^{-3}\text{s}^{-1}$ and $(2.1 \pm 0.8) \times 10^{11} \text{ cm}^{-3}\text{s}^{-1}$, meaning the radiative rate is unchanged. Similar results were found for sample 2 (see Supplemental Material, Fig. S27 and Tables S4 and S5 [21]). Additionally, we previously reported changes in b but constant $\eta_{esc}b_r$ when passivating FAPb_{0.5}Sn_{0.5}I₃ samples of similar thicknesses [28] (Supplemental Material, Table S5 [21]) and have reported variation in b following passivation on MAPbI₃ [33].

Therefore, our results suggest that b can vary between samples (with passivation reducing b) while $\eta_{esc}b_r$ remains constant.

There are several processes which could cause non-radiative second order recombination, including Auger recombination with a trap and processes related to ion motion [34,35]. We suggest it is likely due to excited charges interacting with shallow traps following a Shockley-Read-Hall type process (noting shallow traps have much higher densities, resulting in second order processes) [33,36]. Further work is required to explore this fully.

Calculating device potential of measured films

We demonstrate the power of rapidly extracting decay rates by calculating the efficiency potential for a solar cell fabricated from a measured MAPbI₃ sample. We first measured its absorbance using UV-Vis spectroscopy (another technique accessible to many laboratories), allowing calculation of the fraction of light absorbed (Supplemental Material, Note 10 [21]) and, for the purposes of modelling, fitted an Urbach tail to the low energy edge of this absorbance spectrum [31].

To model a solar cell (or light emitting diode) a measure of the background doping density is required. To calculate this we used the van-Roosbroeck-Shockley relation [37] (for external recombination rates), that

$$n_0p_0 = \frac{\int \pi (a_f(E) + a_b(E)) \phi_{bb}(E) dE}{D\eta_{esc}b_r}. \quad (11)$$

Here n_0 is the background electron density, a_f and a_b the front and back absorbances of the encapsulated sample and ϕ_{bb} the black-body emission flux (per unit area, per unit solid angle, per unit energy). As background carrier density was below instrument resolution in our experiments on halide perovskite films (see Supplemental Material, Note 5 [21]), we assume that $n_0 = p_0$ (i.e. an intrinsic semiconductor), in agreement with several other analyses of MAPbI₃ [38–40]. Additionally, we assume the direct and diffuse absorbances are equal. This approach gives a background carrier density of $1.7 \times 10^5 \text{ cm}^{-3}$, in good agreement with other analyses [20,41]. With this value calculated it is possible to calculate solar cell efficiencies

using the same model as Pazos-Outón et al. [20] but now we also include non-radiative second order processes in the modelling. Finally, we assume the same Auger recombination rate as has been previously measured via TAS [8,42] (though for reasonable values Auger recombination has only a small effect on resulting solar cell efficiencies).

We present predicted current-voltage curves for a device comprised of one of the studied perovskite absorbers in Figure 4a. Specifically, we show the curve for measured decay rates, no first order loss ($a = 0$), no non-radiative second order loss ($\frac{b}{\eta_{esc}b_r} = 1$) and only radiative and Auger recombination (i.e. a fully optimized solar cell). The current voltage curve is almost identical for the measured decay rates and $\frac{b}{\eta_{esc}b_r} = 1$ because first order non-radiative trapping is the dominant loss in these films. Therefore a should be the first process to focus on when optimising solar cells. Once a is reduced the maximum power point voltage can be further increased (by ~ 0.07 V) by reducing second order non-radiative processes.

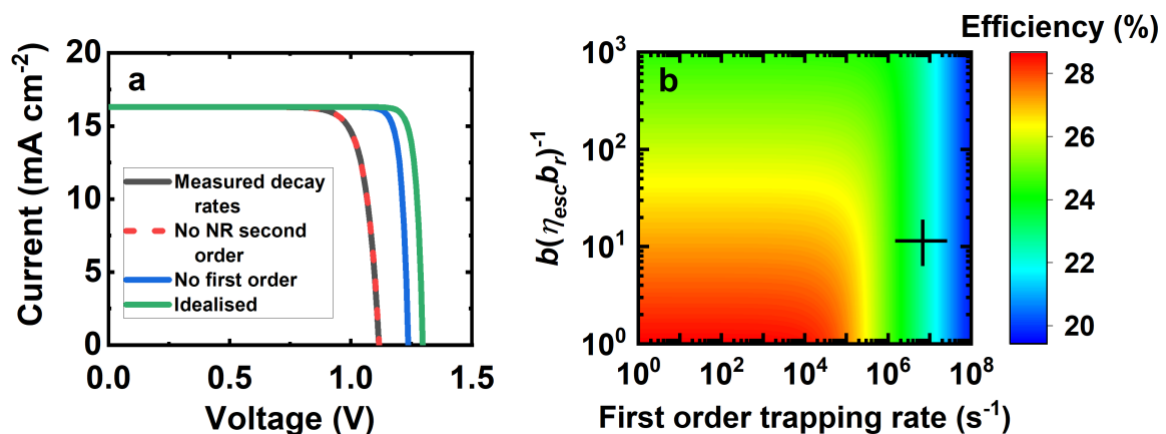


Fig. 4. Predicted solar cell efficiencies for a MAPbI₃ absorber film studied here (sample 3). a) Current-voltage curves for decay rates measured, with no first order loss, no non-radiative (NR) second order loss and the (fully idealized) case of only intrinsic recombination. The solar cell's absorptance is that measured for the encapsulated sample at its given thickness (see Supplemental Material, Note 10 [21]). b) the efficiency of a solar cell made from the same sample, but with optimal absorption, as a function of first order trapping and ratio of total to radiative second order recombination ($\frac{b}{\eta_{esc}b_r}$). The cross marks measured decay rates.

Solar cell efficiency as a function of first and second order recombination rates is plotted for the same absorber layer but with optimal absorption i.e., the sample with a perfect back reflector and no incident light losses, in Figure 4b (noting results are very similar for measured

absorption, Fig. 30). The efficiency achievable with measured trapping rates (cross on figure) is 22.7 %. Removing first order recombination raises this efficiency to 27.2 %, but to obtain the maximum efficiency of 28.6 % second order non-radiative recombination must be reduced. A key conclusion is that when $a < 3 \times 10^5 \text{ s}^{-1}$, second order non-radiative recombination plays an important role in the solar cell. This corresponds to TRPL lifetimes at low excitation density of $\sim 1 \mu\text{s}$, relevant for many halide perovskite thin films [43]. Second order non-radiative recombination plays an even more important role in light-emitting diodes (Fig. S31). Here $\left(\frac{b}{\eta_{esc}b_r}\right)$ needs to be less than 10 to obtain external quantum efficiencies of greater than 20 %. More work is needed to understand non-radiative bimolecular and how it specifically relates to traps, which will in turn allow rational design of passivation approaches that may target trapping, non-radiative bimolecular processes, or both together, to attain optimal halide perovskite device performance.

Conclusion

We have introduced a method for rapidly extracting decay rate ratios from optoelectronic semiconductor thin films on both the bulk and microscale using photoluminescence quantum efficiency measurements. Combining these with time-resolved photoluminescence measurements allows for extraction of all absolute decay rates. We demonstrate that our results are consistent with those obtained from the more infrastructure-intensive transient absorption spectroscopy. Importantly, our measurement approach allows for a direct quantification of second order radiative and total recombination rates. We find that the radiative rate is a fraction of the total second order rate in the range of halide perovskites relevant for photovoltaic application, both at the macro- and micro-scales. We present evidence of the total second order radiative rate changing in thin films with time and passivation, consistent with it relating to carrier traps, while the second order radiative rate remains constant; further work will be required to probe this phenomenon further. Finally, we show how these extracted rates, alongside UV-Vis measurements, allow for the calculation of predicted solar cell efficiencies from the measured samples, and quantify the effect of different decay rates on the limiting efficiency of a solar cell. For our measured sample reducing first order recombination rates should be focused on first, but when time-resolved photoluminescence lifetimes are longer than $1 \mu\text{s}$, attention must be paid to second order non-radiative recombination processes. This work represents a fast method for linking simple spectroscopic measurements to solar cell

performance criteria and revealing recombination pathways, enabling fast screening of potential optoelectronic materials.

Experimental methods

Sample fabrication

For all samples glass substrates and cover slips were cleaned via sonication in acetone and then isopropanol, each for 15 minutes, in an ultrasonic bath. Substrates were then cleaned by UV-Ozone treatment. After substrate cleaning all fabrication steps were in a N₂ filled glovebox.

For MAPbI₃ samples PbI₂ (2 mmol, 0.922 g) and MAI (2 mmol, 0.318 g) was dissolved in 1 mL of DMF: DMSO (4:1) solvent at room temperature with continuous stirring for 30 minutes. This halide perovskite solution was used as a stock solution for making thin films with different thicknesses. Perovskite solution was then dynamically spin coated at 2000 rpm (10 sec) and 4500 rpm (20 sec). Spin coated film were then annealed at 100 °C for 30 minutes. In order to achieve various thicknesses, we diluted the stock solution in following ratios (stock solution = 2.0mmol):

1. Sample 1 = 0.5 mmol (50 μL stock solution + 150 μL of DMF:DMSO);
2. Sample 2 = 0.75 mmol (75 μL stock solution + 125 μL of DMF:DMSO);
3. Sample 3 = 1.0 mmol (100 μL stock solution + 100 μL of DMF:DMSO);
4. Sample 4 = 1.25 mmol (125 μL stock solution + 75 μL of DMF:DMSO).

This produced samples of 230 nm, 270 nm, 330 nm and 760 nm respectively (termed samples 1, 2, 3 and 4 in main text respectively). We spin coated MABF₄ solution in isopropanol (1mg/mL, 4000 rpm, 20 sec) on the surface of annealed perovskite films. All chemicals were purchased from TCI or Greatcell materials.

For Cs_{0.05}FA_{0.79}MA_{0.16}Pb(I_{0.83}Br_{0.17})₃ samples, formamidinium iodide (FAI) (1 M, Greatcell Solar), methylammonium bromide (MABr) (0.2 M, Greatcell Solar), PbI₂ (1.1 M, TCI) and PbBr₂ (0.2 M, TCI) was dissolved in anhydrous dimethylformamide/dimethyl sulfoxide (DMF:DMSO 4:1 (v:v), Sigma). 5% CsI (Sigma) dissolved in DMSO (1.5 M) was then added to the precursor solution. To fabricate the halide perovskite films, 50 μL of prepared solution was spread onto the substrate and spun in a two-step spinning process: 1000 rpm for 10 s and 6000 rpm for 20 s. During the second spinning, 100 μL of chlorobenzene was dropped in the

middle of film 5 s before the end of the process. After spinning, the substrates were transferred to a hotplate and annealed at 100°C for 1 hour.

FASn_{0.5}Pb_{0.5}I₃ samples were prepared following the description in our previous work [28]. Unpassivated and passivated in this work corresponds to 0 % and 5 % content of ZnI₂.

MAPbI₃ and FASn_{0.5}Pb_{0.5}I₃ samples were encapsulated with transparent epoxy immediately following fabrication.

Photoluminescence quantum efficiency

Photoluminescence quantum efficiency (*PLQE*) measurements were recorded using an integrating sphere, following the three measurement approach of De Mello et al. [14]. In both photoluminescence and *PLQE* measurements a continuous wave temperature controlled Thorlabs 520 nm laser was used to photo-excite samples and excitation fluence varied with an optical filter wheel. The emission was recorded using an Andor IDus DU420A Silicon detector. The integrating sphere was regularly cleaned and re-painted, and calibrations were recorded specifically for our measurements.

Time-resolved photoluminescence

Time-resolved PL spectra were recorded using a gated intensified CCD camera (Andor iStar DH740 CCI-010) connected to a calibrated grating spectrometer (Andor SR303i). A Ti:sapphire optical amplifier (1 kHz repetition rate, 90 fs pulse width) was used to generate narrow bandwidth photoexcitation (20 nm full-width at half maximum) with a wavelength of 520 nm, via a custom-built noncollinear optical parametric amplifier (NOPA). We note this NOPA was sometimes a little unstable during measurements, which results in the variations seen in the TRPL results in Figs. S16, S17, S21, S22, S27 and S28.

Transient absorption spectroscopy

For the pump, a TOPAS optical amplifier was pumped with the output from a SpectraPhysics Solstice Ace Ti:Sapphire amplifier (1 kHz) to produce a beam at 520 nm. The probe beam was generated with a LEUKOS Disco 1 UV supercontinuum laser (STM-1-UV, 1 kHz). The probe

was split into a reference and probe and both were focused onto the sample. A pair of line image sensors (Hamamatsu, G11608) mounted on a spectrograph (Andor Solis, Shamrock SR-303i) were used to detect the signal, using a custom-built board from Stresing Entwicklungsburo to read out the signal.

Local PLQE maps

Hyperspectral mapping of perovskite films was performed using an IMATM Vis microscope (Photon etc.). The setup uses a volume Bragg grating that splits light onto a silicon CMOS camera (Hamamatsu) allowing both spatial and spectral resolution of light. Photoluminescence maps were performed using a 405 nm continuous wave laser using a dichroic beam splitter to direct the laser onto the sample and remove the laser from the detected light. In order to calibrate the system for absolute photon counts, first a 658 nm continuous wave laser was coupled into an optical fibre. The laser was reduced in power using several optical density filters into the nW power regime to avoid saturation of the camera. The power of the laser at the end of the fibre was measured using a power meter (Thorlabs). The fibre was then coupled into the objective lens used for the measurements, in this case a Nikon 20 x, 0.45 NA, chromatic aberration corrected objective. The laser spot was imaged and total counts calculated. This gave a conversion between absolute numbers of photons and counts at this wavelength. The objective lens was then coupled into an integrating sphere along with a calibrated white light source (Ocean Insight, HL-3P-INT-CAL). A hyperspectral image of the diffuse light from the integrating sphere was measured to give spatial and spectral sensitivity. Combined with the laser measurement, this gave an absolute calibration of the system.

To measure absolute local photoluminescence quantum efficiency, the total absorbed and emitted photons per second must be calculated at each point. The total incident photon intensity was calculated by measuring both the power and spot size of the 405 nm beam. The reflection spectrum of the sample at 405 nm was found using a white light lamp and calibration mirror with known reflectance. A hyperspectral image of the mirror was measured, dividing the measured spectra at each point of the mirror by the known reflectance spectrum, giving the full incident spectrum of the white light source at each point. The reflection spectrum of the sample was then measured and by dividing by the incident white light spectrum, local absolute reflectance spectra are obtained. While ideally the reflectance at 405 nm would be used to match the laser, the lamp lacked sufficient power and there was low efficiency of the grating

in this region. Therefore, the average value about 450 ± 10 nm is taken. It is assumed that at 405 nm for the sample measured no light is transmitted. Knowing the fraction of light absorbed at each point and the incident intensity, the absorbed photon irradiance can be calculated. After measuring a calibrated hyperspectral photoluminescence maps, and integrating the photoluminescence spectra at each point, the emitted photon irradiance can be found. Dividing the two values point by point gives the local absolute *PLQE*.

Beam size measurements

Spot size was recorded using a Thorlabs beam profiler, with the beam profile being calculated using the Thorlabs beam profile software.

Atomic force microscopy

Sample thickness was recorded using an Asylum Research MFP-3D atomic force microscope in non-contact AC mode. A scratch on the surface on an unencapsulated sample was made using metal tweezers and the average difference in height between the material surface and the glass below as recorded (after 0th order flattening and 1st order plane fit were applied). All measurements and data processing were carried out on Asylum Research AFM Software version 15.

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Conflicts of Interest

SDS is a co-founder of Swift Solar Inc.

Data availability

The data underlying this manuscript are available at [url to be added in proof].

Code availability

The codes used in this work are available at [url to be added in proof].

References

- [1] M. A. Green, A. Ho-Baillie, and H. J. Snaith, *The Emergence of Perovskite Solar Cells*, *Nature Photonics* **8**, 506 (2014).
- [2] Z.-K. Tan, R. S. Moghaddam, M. L. Lai, P. Docampo, R. Higler, F. Deschler, M. Price, A. Sadhanala, L. M. Pazos, D. Credgington, F. Hanusch, T. Bein, H. J. Snaith, and R. H. Friend, *Bright Light-Emitting Diodes Based on Organometal Halide Perovskite*, *Nature Nanotechnology* **9**, 687 (2014).
- [3] Y. Zhou, J. Chen, O. M. Bakr, and O. F. Mohammed, *Metal Halide Perovskites for X-Ray Imaging Scintillators and Detectors*, *ACS Energy Letters* **6**, 739 (2021).
- [4] L. J. Phillips, C. N. Savory, O. S. Hutter, P. J. Yates, H. Shiel, S. Mariotti, L. Bowen, M. Birkett, K. Durose, D. O. Scanlon, and J. D. Major, *Current Enhancement via a TiO Window Layer for CSS Sb₂Se₃ Solar Cells: Performance Limits and High VOC*, *IEEE Journal of Photovoltaics* **9**, 544 (2019).
- [5] L. C. Lee, T. N. Huq, J. L. Macmanus-Driscoll, and R. L. Z. Hoyer, *Research Update: Bismuth-Based Perovskite-Inspired Photovoltaic Materials*, *APL Materials* **6**, 084502 (2018).
- [6] National Renewable Energy Laboratory (NREL), *Best Research Cell Efficiencies*, <https://www.nrel.gov/pv/assets/pdfs/best-research-cell-efficiencies.20200203.pdf>.
- [7] T. W. Crothers, R. L. Milot, J. B. Patel, E. S. Parrott, J. Schlipf, P. Müller-Buschbaum, M. B. Johnston, and L. M. Herz, *Photon Reabsorption Masks Intrinsic Bimolecular Charge-Carrier Recombination in CH₃NH₃PbI₃ Perovskite*, *Nano Letters* **17**, 5782 (2017).
- [8] J. M. Richter, M. Abdi-Jalebi, A. Sadhanala, M. Tabachnyk, J. P. H. Rivett, L. M. Pazos-Outón, K. C. Gödel, M. Price, F. Deschler, and R. H. Friend, *Enhancing Photoluminescence Yields in Lead Halide Perovskites by Photon Recycling and Light Out-Coupling*, *Nature Communications* **7**, 13941 (2016).
- [9] M. G. Christoforo, E. T. Hoke, M. D. McGehee, and E. L. Unger, *Transient Response of Organo-Metal-Halide Solar Cells Analyzed by Time-Resolved Current-Voltage Measurements*, *Photonics* **2**, 1101 (2015).
- [10] A. Pockett, G. E. Eperon, T. Peltola, H. J. Snaith, A. Walker, L. M. Peter, and P. J. Cameron, *Characterization of Planar Lead Halide Perovskite Solar Cells by Impedance Spectroscopy, Open-Circuit Photovoltage Decay, and Intensity-Modulated Photovoltage/Photocurrent Spectroscopy*, *Journal of Physical Chemistry C* **119**, 3456 (2015).
- [11] D. W. deQuilettes, K. Frohna, D. Emin, T. Kirchartz, V. Bulovic, D. S. Ginger, and S. D. Stranks, *Charge-Carrier Recombination in Halide Perovskites*, *Chemical Reviews* **119**, 11007 (2019).
- [12] A. Kiligaris, P. A. Frantsuzov, A. Yangui, S. Seth, J. Li, Q. An, Y. Vaynzof, and I. G. Scheblykin, *Are Shockley-Read-Hall and ABC Models Valid for Lead Halide Perovskites?*, *Nature Communications* **12**, 3329 (2021).
- [13] T. A. S. Doherty, A. J. Winchester, S. Macpherson, D. N. Johnstone, V. Pareek, E. M. Tennyson, S. Kosar, F. U. Kosasih, M. Anaya, M. Abdi-Jalebi, Z. Andaji-Garmaroudi, E. L. Wong, J. Madéo, Y. H. Chiang, J. S. Park, Y. K. Jung, C. E. Petoukhoff, G. Divitini, M. K. L. Man, C. Ducati, A. Walsh, P. A. Midgley, K. M. Dani, and S. D. Stranks, *Performance-Limiting Nanoscale Trap Clusters at Grain Junctions in Halide Perovskites*, *Nature* **580**, 360 (2020).
- [14] J. C. De Mello, H. F. Wittmann, and R. H. Friend, *An Improved Experimental Determination of External Photoluminescence Quantum Efficiency*, *Advanced Materials* **9**, 230 (1997).
- [15] S. D. Stranks, *Nonradiative Losses in Metal Halide Perovskites*, *ACS Energy Letters* **2**, 1515 (2017).
- [16] M. J. Trimpl, A. D. Wright, K. Schutt, L. R. V. V. Buizza, Z. Wang, M. B. Johnston, H. J. Snaith, P. Müller-Buschbaum, and L. M. Herz, *Charge-Carrier Trapping and Radiative Recombination in Metal Halide Perovskite Semiconductors*, *Advanced Functional Materials* **30**, 2004312 (2020).
- [17] L. L. Kerr, S. S. Li, S. W. Johnston, T. J. Anderson, O. D. Crisalle, W. K. Kim, J. Abushama, and R. N. Noufi, *Investigation of Defect Properties in Cu(In,Ga)Se₂ Solar Cells by Deep-Level Transient Spectroscopy*, *Solid-State Electronics* **48**, 1579 (2004).

- [18] S. D. Stranks, G. E. Eperon, G. Grancini, C. Menelaou, M. J. P. Alcocer, T. Leijtens, L. M. Herz, A. Petrozza, and H. J. Snaith, *Electron-Hole Diffusion Lengths Exceeding 1 Micrometer in an Organometal Trihalide Perovskite Absorber*, *Science* **342**, 341 (2013).
- [19] Y. Yang, M. Yang, D. T. Moore, Y. Yan, E. M. Miller, K. Zhu, and M. C. Beard, *Lead Iodide Perovskite Films*, *Nature Energy* **2**, 16207 (2017).
- [20] L. M. Pazos-Outón, T. P. Xiao, and E. Yablonovitch, *Fundamental Efficiency Limit of Lead Iodide Perovskite Solar Cells*, *The Journal of Physical Chemistry Letters* **9**, 1703 (2018).
- [21] *See Supplemental Material at [URL Will Be Inserted by Publisher] for i) Definition of All Algebraic Terms Used, ii) Five Notes Giving Additional Details on Fitting Procedures, iii) Three Notes on Microscopic PLQE Data, iv) One Note on UV-Vis Data, v) Tables listing all fitted parameters and vi) additional figures supporting the main text.*
- [22] S. Nagane, S. Macpherson, M. A. Hope, D. J. Kubicki, W. Li, S. D. Verma, J. Ferrer Orri, Y. H. Chiang, J. L. MacManus-Driscoll, C. P. Grey, and S. D. Stranks, *Tetrafluoroborate-Induced Reduction in Defect Density in Hybrid Perovskites through Halide Management*, *Advanced Materials* 2102462 (2021).
- [23] S. D. Stranks, V. M. Burlakov, T. Leijtens, J. M. Ball, A. Goriely, and H. J. Snaith, *Recombination Kinetics in Organic-Inorganic Perovskites: Excitons, Free Charge, and Subgap States*, *Physical Review Applied* **2**, 034007 (2014).
- [24] T. Leijtens, G. E. Eperon, A. J. Barker, G. Grancini, W. Zhang, J. M. Ball, A. R. S. Kandada, H. J. Snaith, and A. Petrozza, *Carrier Trapping and Recombination: The Role of Defect Physics in Enhancing the Open Circuit Voltage of Metal Halide Perovskite Solar Cells*, *Energy Environ. Sci.* **9**, 3472 (2016).
- [25] L. M. Pazos-Outón, T. P. Xiao, and E. Yablonovitch, *Fundamental Efficiency Limit of Lead Iodide Perovskite Solar Cells*, *J. Phys. Chem. Lett.* **9**, 1703 (2018).
- [26] E. M. Tennyson, T. A. S. Doherty, and S. D. Stranks, *Heterogeneity at Multiple Length Scales in Halide Perovskite Semiconductors*, *Nature Reviews Materials* **4**, 573 (2019).
- [27] R. Berera, R. van Grondelle, and J. T. M. Kennis, *Ultrafast Transient Absorption Spectroscopy: Principles and Application to Photosynthetic Systems*, *Photosynthesis Research* **101**, 105 (2009).
- [28] A. R. Bowman, M. T. Klug, T. A. S. Doherty, M. D. Farrar, S. P. Senanayak, B. Wenger, G. Divitini, E. P. Booker, Z. Andaji-Garmaroudi, S. Macpherson, E. Ruggeri, H. Sirringhaus, H. J. Snaith, and S. D. Stranks, *Microsecond Carrier Lifetimes, Controlled p-Doping, and Enhanced Air Stability in Low-Bandgap Metal Halide Perovskites*, *ACS Energy Letters* **4**, 2301 (2019).
- [29] F. Staub, T. Kirchartz, K. Bittkau, and U. Rau, *Manipulating the Net Radiative Recombination Rate in Lead Halide Perovskite Films by Modification of Light Outcoupling*, *Journal of Physical Chemistry Letters* **8**, 5084 (2017).
- [30] K. Frohna, M. Anaya, S. Macpherson, J. Sung, T. A. S. Doherty, Y. H. Chiang, A. J. Winchester, K. W. P. Orr, J. E. Parker, P. D. Quinn, K. M. Dani, A. Rao, and S. D. Stranks, *Nanoscale Chemical Heterogeneity Dominates the Optoelectronic Response of Alloyed Perovskite Solar Cells*, *Nature Nanotechnology* (2021). DOI: 10.1038/s41565-021-01019-7
- [31] A. R. Bowman, M. Anaya, N. C. Greenham, and S. D. Stranks, *Quantifying Photon Recycling in Solar Cells and Light-Emitting Diodes: Absorption and Emission Are Always Key*, *Physical Review Letters* **125**, 067401 (2020).
- [32] M. Anaya, J. F. Galisteo-López, M. E. Calvo, J. P. Espinós, and H. Míguez, *Origin of Light-Induced Photophysical Effects in Organic Metal Halide Perovskites in the Presence of Oxygen*, *Journal of Physical Chemistry Letters* **9**, 3891 (2018).
- [33] R. Brenes, D. Guo, A. Osherov, N. K. Noel, C. Eames, E. M. Hutter, S. K. Pathak, F. Niroui, R. H. Friend, M. S. Islam, H. J. Snaith, V. Bulović, T. J. Savenije, and S. D. Stranks, *Metal Halide Perovskite Polycrystalline Films Exhibiting Properties of Single Crystals*, *Joule* **1**, 155 (2017).
- [34] F. Staub, U. Rau, and T. Kirchartz, *Statistics of the Auger Recombination of Electrons and Holes via Defect Levels in the Band Gap - Application to Lead-Halide Perovskites*, *ACS Omega* **3**, 8009 (2018).

- [35] P. T. Landsberg, C. Rhys-Roberts, and P. Lal, *Auger Recombination and Impact Ionization Involving Traps in Semiconductors*, Proc. Phys. Soc. **84**, 915 (1964).
- [36] H. Xie, Z. Wang, Z. Chen, C. Pereyra, M. Pols, K. Gałkowski, M. Anaya, S. Fu, X. Jia, P. Tang, D. J. Kubicki, A. Agarwalla, H. S. Kim, D. Prochowicz, X. Borrísé, M. Bonn, C. Bao, X. Sun, S. M. Zakeeruddin, L. Emsley, J. Arbiol, F. Gao, F. Fu, H. I. Wang, K. J. Tielrooij, S. D. Stranks, S. Tao, M. Grätzel, A. Hagfeldt, and M. Lira-Cantu, *Decoupling the Effects of Defects on Efficiency and Stability through Phosphonates in Stable Halide Perovskite Solar Cells*, Joule **5**, 1246 (2021).
- [37] W. van Roosbroeck and W. Shockley, *Photon-Radiative Recombination of Electrons and Holes in Germanium*, Physical Review **94**, 1558 (1954).
- [38] S. Feldmann, S. Macpherson, S. P. Senanayak, M. Abdi-Jalebi, J. P. H. Rivett, G. Nan, G. D. Tainter, T. A. S. Doherty, K. Frohna, E. Ringe, R. H. Friend, H. Sirringhaus, M. Saliba, D. Beljonne, S. D. Stranks, and F. Deschler, *Photodoping through Local Charge Carrier Accumulation in Alloyed Hybrid Perovskites for Highly Efficient Luminescence*, Nature Photonics **14**, 123 (2020).
- [39] L. Krückemeier, B. Krogmeier, Z. Liu, U. Rau, and T. Kirchartz, *Understanding Transient Photoluminescence in Halide Perovskite Layer Stacks and Solar Cells*, Advanced Energy Materials **11**, 2003489 (2021).
- [40] Z. Ni, C. Bao, Y. Liu, Q. Jiang, W.-Q. Wu, S. Chen, X. Dai, B. Chen, B. Hartweg, Z. Yu, Z. Holman, and J. Huang, *Resolving Spatial and Energetic Distributions of Trap States in Metal Halide Perovskite Solar Cells*, Science **367**, 1352 (2020).
- [41] F. Staub, H. Hempel, J. C. Hebig, J. Mock, U. W. Paetzold, U. Rau, T. Unold, and T. Kirchartz, *Beyond Bulk Lifetimes: Insights into Lead Halide Perovskite Films from Time-Resolved Photoluminescence*, Physical Review Applied **6**, 044017 (2016).
- [42] J. X. Shen, X. Zhang, S. Das, E. Kioupakis, and C. G. Van de Walle, *Unexpectedly Strong Auger Recombination in Halide Perovskites*, Advanced Energy Materials **8**, 1801027 (2018).
- [43] D. W. deQuilettes, S. Koch, S. Burke, R. K. Paranj, A. J. Shropshire, M. E. Ziffer, and D. S. Ginger, *Photoluminescence Lifetimes Exceeding 8 Ms and Quantum Yields Exceeding 30 % in Hybrid Perovskite Thin Films by Ligand Passivation*, ACS Energy Letters **1**, 438 (2016).